

Integrujte

$$(1) \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \sin^2(x) - \frac{1}{\sin^2(x)} \, dx$$

$$(2) \int_0^{\pi} x \sin(2x) \, dx.$$

$$(3) \int_0^1 x \operatorname{arctg}(x) \, dx.$$

$$(4) \int_1^e \frac{\ln(x)}{x (\ln^2(x) + 4)} \, dx.$$

$$(5) \int_0^1 (x - 1) e^x \, dx.$$

$$(6) \int_0^{\frac{\pi}{4}} \operatorname{tg}^3 x \, dx.$$

$$(7) \int_0^1 \frac{x+2}{x+1} \, dx$$

$$(8) \int_0^1 x \sqrt{x^2 + 1} \, dx$$

$$(9) \int_0^{\pi^2} \sin \sqrt{x} \, dx.$$

$$(10) \int_1^e \frac{\ln(x)}{x^2} \, dx.$$

$$(11) \int_1^e x^2 \ln(x) \, dx.$$

$$(12) \int_0^{\frac{\pi}{4}} \frac{\sin^3(x) + 2}{\cos^2(x)} \, dx.$$

$$(13) \int_0^{\frac{\sqrt{\pi}}{2}} x \operatorname{tg}(x^2) \, dx.$$

$$(14) \int_0^{\frac{\pi}{2}} \frac{\sin(2x)}{1 + \cos^2(x)} \, dx$$

$$(15) \int_{e^{\frac{\pi}{2}}}^{e^{\pi}} \frac{\sin(\ln(x))}{x} \, dx.$$

$$(16) \int_0^{\frac{\pi}{4}} \frac{x}{\cos^2(x)} \, dx.$$

$$(17) \int_0^1 \sqrt[3]{x \sqrt{x^3}} \, dx$$

$$(18) \int_1^{e^2} x \ln(\sqrt{x}) \, dx.$$

$$(19) \int_0^1 x \sin(1 - x^2) \, dx.$$

$$(20) \int_0^{\pi} \sin^3(x) \, dx.$$

$$(21) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} x \cos\left(\frac{x}{2}\right) \, dx.$$

$$(22) \int_0^{\frac{\pi}{4}} \operatorname{tg}^2(x) \, dx$$

$$(23) \int_1^e \ln^2(x) \, dx.$$

$$(30) \int_0^1 \frac{\sqrt{x}-1}{\sqrt{x}+1} \, dx.$$

$$(24) \int_1^e \frac{1}{x \left(\ln^2(x) + 4 \right)} \, dx.$$

$$(31) \int_0^1 \frac{x}{\sqrt{x}+1} \, dx.$$

$$(25) \int_0^{\frac{\sqrt{\pi}}{2}} \frac{x}{\cotg(x^2)} \, dx.$$

$$(32) \int_0^1 \arccos(x) \, dx.$$

$$(26) \int_1^e x \ln^2(x) \, dx.$$

$$(33) \int_0^1 x \ln(x+1) \, dx.$$

$$(27) \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \cos(x) \ln(\sin(x)) \, dx.$$

$$(34) \int_0^1 \frac{\sqrt{x}}{x+1} \, dx.$$

$$(28) \int_{-1}^1 x^2 e^{-x} \, dx.$$

$$(35) \int_0^{\frac{\pi}{3}} \cos^2(x) - \frac{1}{\cos^2(x)} \, dx$$

$$(29) \int_0^{\pi} x^2 \cos\left(\frac{x}{2}\right) \, dx$$

$$(36) \int_0^1 \frac{x}{1+x^4} \, dx$$

Integrujte

$$(1) \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \sin^2(x) - \frac{1}{\sin^2(x)} dx = \frac{1}{8} (\pi - 6).$$

$$(2) \int_0^{\pi} x \sin(2x) dx = -\frac{\pi}{2}.$$

$$(3) \int_0^1 x \operatorname{arctg}(x) dx = \frac{1}{4} (\pi - 2).$$

$$(4) \int_1^e \frac{\ln(x)}{x (\ln^2(x) + 4)} dx = \frac{1}{2} \ln\left(\frac{5}{4}\right).$$

$$(5) \int_0^1 (x - 1) e^x dx = 2 - e.$$

$$(6) \int_0^{\frac{\pi}{4}} \operatorname{tg}^3 x dx = \frac{1}{2} (1 - \ln(2)).$$

$$(7) \int_0^1 \frac{x+2}{x+1} dx = 1 + \ln 2.$$

$$(8) \int_0^1 x \sqrt{x^2 + 1} dx = \frac{1}{3} (\sqrt{2} - 1).$$

$$(9) \int_0^{\pi^2} \sin \sqrt{x} dx = 2\pi.$$

$$(10) \int_1^e \frac{\ln(x)}{x^2} dx = \frac{e-2}{e}.$$

$$(11) \int x^2 \ln(x) dx = \frac{1}{9} (2e^3 + 1).$$

$$(12) \int_0^{\frac{\pi}{4}} \frac{\sin^3(x) + 2}{\cos^2(x)} dx = \frac{3\sqrt{2}}{2}.$$

$$(13) \int_0^{\frac{\sqrt{\pi}}{2}} x \operatorname{tg}\left(x^2\right) dx = \frac{\ln(2)}{4}.$$

$$(14) \int_0^{\frac{\pi}{2}} \frac{\sin(2x)}{1+\cos^2(x)} dx = \ln 2.$$

$$(15) \int \frac{\sin(\ln(x))}{x} dx = -\cos(\ln(x)) + c = -\cos(\ln(x)) + c.$$

$$(16) \int_0^{\frac{\pi}{4}} \frac{x}{\cos^2(x)} dx = \frac{1}{4}(\pi - \ln(4)).$$

$$(17) \int_0^1 \sqrt[3]{x\sqrt{x^3}} dx = \frac{6}{11}.$$

$$(18) \int x \ln(\sqrt{x}) dx = \frac{1}{8} \left(1 + 3e^4\right)$$

$$(19) \int_0^1 x \sin\left(1-x^2\right) dx = \frac{1}{2} \left(1 - \cos(1)\right).$$

$$(20) \int_0^{\pi} \sin^3(x) dx = \frac{4}{3}.$$

$$(21) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} x \cos\left(\frac{x}{2}\right) dx = 0.$$

$$(22) \int_0^{\frac{\pi}{4}} \operatorname{tg}^2(x) dx = 1 - \frac{\pi}{4}.$$

$$(23) \int_1^e \ln^2(x) dx = e - 2.$$

$$(24) \int_1^e \frac{1}{x\left(\ln^2(x)+4\right)} dx = \frac{1}{2} \operatorname{arctg}\left(\frac{1}{2}\right).$$

$$(25) \quad \int_0^{\frac{\sqrt{\pi}}{2}} \frac{x}{\cotg(x^2)} \, dx = \frac{\ln(2)}{4}.$$

$$(26) \quad \int_1^e x \ln^2(x) \, dx = \frac{1}{4} (e^2 - 1).$$

$$(27) \quad \int \cos(x) \ln(\sin(x)) \, dx = 1 - \left(\frac{\sqrt{2}}{2} \ln \left| \frac{\sqrt{2}}{2} \right| - \frac{\sqrt{2}}{2} \right).$$

$$(28) \quad \int_{-1}^1 x^2 e^{-x} \, dx = e - \frac{5}{e}.$$

$$(29) \quad \int_0^{2\pi} x^2 \cos\left(\frac{x}{2}\right) \, dx = -16\pi.$$

$$(30) \quad \int_0^1 \frac{\sqrt{x} - 1}{\sqrt{x} + 1} \, dx = 4 \ln 2 - 3.$$

$$(31) \quad \int_0^1 \frac{x}{\sqrt{x} + 1} \, dx = \frac{5}{3} - 2 \ln(2).$$

$$(32) \quad \int_0^1 \arccos(x) \, dx = 1.$$

$$(33) \quad \int_0^1 x \ln(x + 1) \, dx = \frac{1}{4}.$$

$$(34) \quad \int_0^1 \frac{\sqrt{x}}{x + 1} \, dx = 2 - \frac{\pi}{2}.$$

$$(35) \quad \int_0^{\frac{\pi}{3}} \cos^2(x) - \frac{1}{\cos^2 x} \, dx = \frac{\pi}{6} - \frac{7\sqrt{3}}{8}.$$

$$\int_0^1 \frac{x}{1 + x^4} \, dx = \frac{\pi}{8}.$$