

Vyřešte v $\mathbb{R}$ rovnici, proveďte zkoušku

$$1. \quad \sqrt{4+x}\sqrt{x^2-7}=x$$

$$2. \quad \sqrt{2x+3}-\sqrt{x^2-5}=x-2$$

$$3. \quad \frac{\sqrt{x+13}+2}{\sqrt{x+13}-4}=7$$

$$4. \quad 1+\sqrt{1+x}\sqrt{x^2-24}=x$$

$$5. \quad \sqrt{x+1}+2\sqrt{2x+1}=3\sqrt{3x+1}$$

$$6. \quad \sqrt{1+x}=\frac{11-x}{\sqrt{2+3x}}$$

$$7. \quad 1-\sqrt{1-x}\sqrt{x^2+24}=x$$

$$8. \quad \frac{\sqrt{x-1}+1}{1-\sqrt{x+1}}=-3$$

$$9. \quad \frac{\sqrt{5x+4}+2}{\sqrt{3x+1}-1}=5$$

$$10. \quad \sqrt{x+1}=x+\sqrt{x^2+1}$$

$$11. \quad \sqrt{2+x}+\sqrt{x}=\frac{4}{\sqrt{2+x}}$$

$$12. \quad \sqrt{2+x}+\sqrt{2-x}=\sqrt{3+x^2}$$

$$13. \quad \sqrt{3x+1}-\sqrt{3+x}=4$$

$$14. \quad -1+\sqrt{2x+\sqrt{2x^2+1}}=x$$

$$15. \quad \frac{2+\sqrt{2x-1}}{4-\sqrt{2x-1}}=8-\sqrt{2x-1}$$

$$16. \quad \frac{\sqrt{2}-\sqrt{x}}{2-x}=\sqrt{\frac{1}{2-x}}$$

$$17. \quad \frac{1+\sqrt{x+2}}{3+\sqrt{x-2}}=1$$

$$18. \quad \sqrt{x+10}=5-\sqrt{x+5}$$

$$19. \quad \sqrt{3+x}+\sqrt{1+3x}=4$$

$$20. \quad \sqrt{x+1}+\sqrt{x-1}=\sqrt{3x-1}$$

$$21. \quad \sqrt{1+x}=\frac{x}{\sqrt{2+3x}}$$

$$22. \quad 1=\sqrt{1+3x}+\sqrt{2+3x}$$

$$23. \quad \frac{1-\sqrt{2x+3}}{\sqrt{2x+3}-4}=2$$

$$24. \quad 2-\sqrt{x+3}=1+\sqrt{2+x}$$

$$25. \quad \sqrt{x}=\sqrt{2x+1}-\sqrt{3x-1}$$

Vyřešte v $\mathbb{R}$ rovnici, proveďte zkoušku

1.
 $x = 4,$

2.
 $x = 3,$

3.
 $x = 12,$

4.
 $x = 7,$

5.
 $x = 0,$

6.
 $x_1 = \frac{7}{2},$

7.
 $x_1 = 0, x_2 = -5,$

8.
 $x = \frac{5}{4},$

9.
 $x = 1,$

10.
 $x_1 = 0, x_2 = -\frac{3}{4},$

11.
 $x = \frac{2}{3},$

12.
 $x_{1,2} = \pm\sqrt{3},$

13.
 $x = 33,$

14.
 $x = 0,$

15.
 $x_1 = 5, x_2 = \frac{101}{2},$

16.
 $x = 0,$

17.
 $x = 2,$

18.
 $x = -1,$

19.
 $x = 1,$

20.
 $x = 1,$

21.
nemá řešení,

22.
 $x = -\frac{1}{3}$

23.
 $x = 3,$

24.
 $x = -2,$

25.
 $x_1 = \frac{1}{2},$