

Vyřešte v $\mathbb{R}$ rovnici, proveďte zkoušku

1.
$$\frac{1}{\cos^2 x} - \operatorname{tg}^2 x = 1$$

2.
$$\frac{1 + \sin x}{\cos x} + \frac{\cos x}{1 - \sin x} = \cos x$$

3.
$$\frac{1}{\sin x} - \operatorname{cotg} x = 1$$

4.
$$\operatorname{tg} x + \operatorname{cotg} x = 2$$

5.
$$\cos 2x + 4 \sin^2 x = 3$$

6.
$$\cos x = \frac{\sin 2x}{2}$$

7.
$$\sin 2x = -\operatorname{cotg} x$$

8.
$$\sin^3 x + \cos^3 x = 1$$

9.
$$\sin \frac{x}{2} = \cos x$$

10.
$$\frac{\sin x}{1 - \cos 2x} = \cos x$$

11.
$$4 \cos 3x + 5 \sin^2 3x = -4$$

12.
$$\frac{1 + \sin x}{\cos x} + \frac{\cos x}{1 + \sin x} = 2 \sin x$$

13.
$$\cos 2x - 9 \sin x = 8$$

14.
$$1 - \sin x = \cos 2x$$

15.
$$2 \cos \frac{x}{2} = \sin x$$

16.
$$\cos 2x - \sin 2x = 1$$

17.
$$\cos x - \operatorname{tg}^2 x = 1$$

18.
$$\cos \frac{x}{2} = \sin x$$

19.
$$\sin \left(x + \frac{\pi}{6} \right) + \sin \left(x - \frac{\pi}{6} \right) = \frac{\sqrt{3}}{2}$$

20.
$$\cos \left(x + \frac{\pi}{3} \right) + \cos \left(x - \frac{\pi}{6} \right) = 1$$

21.
$$2 \cos 2x = \sin 4x$$

22.
$$\sin^4 x - \cos^4 x = 1$$

23.
$$\cos^2 x + 3 \sin x = 1$$

24.
$$\frac{\sin x}{1 - \cos x} + \frac{1 + \cos x}{\sin x} = 2$$

25.
$$\operatorname{cotg} 2x + \operatorname{tg} x = 1$$

Vyřešte v $\mathbb{R}$ rovnici, proveďte zkoušku

1. $x \neq (2k+1) \frac{\pi}{2}, k \in \mathbb{Z},$
2. nemá řešení,
3. $x = \frac{\pi}{2} + 2k\pi, k \in \mathbb{Z},$
4. $x = \frac{\pi}{4} + k\pi, k \in \mathbb{Z},$
5. $x = \frac{\pi}{2} + k\pi; k \in \mathbb{Z};$
6. $x = (2k+1) \frac{\pi}{2}, k \in \mathbb{Z},$
7. $x = (2k+1) \frac{\pi}{2}, k \in \mathbb{Z},$
8. $x_1 = \frac{\pi}{2} + 2k\pi, x_2 = 2k\pi, k \in \mathbb{Z},$
9. $x_1 = \frac{\pi}{3} + 4k\pi, x_2 = \frac{5\pi}{3} + 4k\pi, x_3 = -\pi + 4k\pi, k \in \mathbb{Z},$
10. $x = \frac{\pi}{4} + k\pi,$
11. $x = (2k+1) \frac{\pi}{3}, k \in \mathbb{Z}$
12. nemá řešení,
13. $x = -\frac{\pi}{2} + 2k\pi; k \in \mathbb{Z};$
14. $x_1 = \frac{\pi}{6} + 2k\pi, x_2 = \frac{5\pi}{6} + 2k\pi, x_3 = k\pi, k \in \mathbb{Z},$
15. $x = (2k+1) \pi, k \in \mathbb{Z},$
16. $x_1 = \frac{\pi}{4} + k\pi; k \in \mathbb{Z}, x_2 = k\pi; k \in \mathbb{Z};$
17. $x = 2k\pi, k \in \mathbb{Z},$
18. $x_1 = \frac{\pi}{3} + 4k\pi, x_2 = \frac{5\pi}{3} + 4k\pi, x_3 = (2k+1) \pi, k \in \mathbb{Z},$
19. $x_1 = \frac{\pi}{6} + 2k\pi, x_2 = \frac{5\pi}{6} + 2k\pi, k \in \mathbb{Z},$
20. $x_1 = \frac{\pi}{6} + 2k\pi, x_2 = -\frac{\pi}{3} + 2k\pi, k \in \mathbb{Z},$
21. $x = (2k+1) \frac{\pi}{4}, k \in \mathbb{Z},$
22. $x = \frac{\pi}{2} + k\pi, k \in \mathbb{Z},$
23. $x = k\pi; k \in \mathbb{Z};$
24. $x = \frac{\pi}{2} + k\pi,$
25. $x = \frac{\pi}{4} + k\pi, k \in \mathbb{Z},$