

Spočtěte derivaci funkce $f(x)$:

1.

$$f(x) = \left(x - \frac{x^2}{x+1} \right)^{-1}$$

2.

$$f(x) = \left(\frac{1}{x-1} - \frac{x}{x^2-1} \right)^{-1}$$

3.

$$f(x) = \frac{\frac{x+1}{x-1} - \frac{x-1}{x+1}}{1 - \frac{x^2+1}{x^2-1}}$$

4.

$$f(x) = \frac{\frac{2x}{x+1} - x}{1 - \frac{2x}{x+1}}$$

5.

$$f(x) = \sqrt{x\sqrt{x\sqrt{x}}}$$

6.

$$f(x) = \frac{\frac{1-\sqrt{x}}{x^{-2}}}{1+\sqrt{x}}$$

7.

$$f(x) = \frac{\frac{x^{-2}}{x-3} - \frac{x+3}{x}}{x-3}$$

8.

$$f(x) = \left(\frac{1}{x+1} - \frac{2x}{x^2-1} \right)^{-1}$$

9.

$$f(x) = \frac{\sqrt[3]{x^2\sqrt{x}}}{\sqrt[4]{x^3\sqrt{x}}}$$

10.

$$f(x) = \left(\frac{\frac{1}{x^2} - 1}{x - \frac{1}{x}} \right)^{-2}$$

11.

$$f(x) = \left(\frac{1}{x-1} - \frac{x}{x^2+x-2} \right)^{-1}$$

12.

$$f(x) = \frac{\frac{\sqrt{x^3}}{\sqrt[3]{x}}}{\frac{\sqrt[3]{x^2}}{\sqrt{x}}}$$

13.

$$f(x) = \sqrt[4]{x^3\sqrt{x\sqrt{x}}}$$

14.

$$f(x) = \frac{x - \frac{1}{x}}{\frac{1}{x^{-2}}}$$

15.

$$f(x) = \frac{\frac{\sqrt{x}}{\sqrt{x}-1} - \frac{1}{\sqrt{x}+1} + 1}{\frac{\sqrt{x}}{\sqrt{x}+1} + \frac{1}{\sqrt{x}-1} - 1}$$

16.

$$f(x) = \left(\frac{1}{x-1} - \frac{x}{x^2-x+1} \right)^{-1}$$

17.

$$f(x) = \frac{x^{-1}}{\frac{x}{3-x} + \frac{x+3}{x}}$$

18.

$$f(x) = \frac{\sqrt[3]{x^2} - \sqrt{x^3}}{\frac{1}{x}}$$

19.

$$f(x) = \frac{\sqrt{x^3\sqrt[4]{x^5}}}{\sqrt[3]{x\sqrt{x}}}$$

20.

$$f(x) = \frac{\sqrt{x} - \sqrt[3]{x^2}}{\sqrt[4]{x^3}}$$

21.

$$f(x) = \frac{\frac{1}{x} - 1}{x - \frac{1}{x}}$$

22.

$$f(x) = \frac{\sqrt[3]{x^4} \sqrt{x^3}}{\sqrt{x^3} \sqrt[3]{x^2}}.$$

23.

$$f(x) = \left(\frac{2x}{2-x} - x \right) \cdot \frac{2}{1 - \frac{x}{x-2}}$$

24.

$$f(x) = \left(\frac{1 + \frac{1}{x}}{\frac{1}{x} - x} \right)^{-1}$$

25.

$$f(x) = \sqrt{x \sqrt[3]{x \sqrt[4]{x}}}.$$

Spočtěte derivaci funkce $f(x)$:

1.
 $f'(x) = -\frac{1}{x^2}$

2.
 $f'(x) = 2x$

3.
 $f'(x) = -2$

4.
 $f'(x) = 1$

5.
 $f'(x) = \frac{7}{8}x^{-\frac{1}{8}}$

6.
 $f'(x) = 1 - 2x$

7.
 $f'(x) = \frac{1}{3}x^{-2}$

8.
 $f'(x) = -1$

9.
 $f'(x) = -\frac{1}{24}x^{-\frac{25}{24}}$

10.
 $f'(x) = 2x$

11.
 $f'(x) = \frac{1}{2}(2x + 1)$

12.
 $f'(x) = 1$

13.
 $f'(x) = \frac{3}{8}x^{-\frac{5}{8}}$

14.
 $f'(x) = -x^{-2} + 3x^{-4}$

15.
 $f'(x) = 1$

16.
 $f'(x) = -2(x - 1)$

17.
 $f'(x) = -\frac{1}{9}$

18.
 $f'(x) = \frac{5}{3}x^{\frac{2}{3}} - \frac{5}{2}x^{\frac{3}{2}}$

19.
 $f'(x) = \frac{13}{8}x^{\frac{5}{8}}$

20.
 $f'(x) = -\frac{1}{4}x^{-\frac{5}{4}} + \frac{1}{12}x^{-\frac{13}{12}}$

21.
 $f'(x) = (x + 1)^{-2}$

22.
 $f'(x) = 0.$

23.
 $f'(x) = 2x$

24.
 $f'(x) = -1$

25.
 $f'(x) = \frac{17}{24}x^{-\frac{7}{24}}$