

Vyřešte soustavu rovnic

1.

$$\begin{aligned} 2x_1 + x_3 - x_4 &= 2 \\ 3x_1 + x_2 + 2x_3 &= 2 \\ 2x_1 - 3x_2 + x_4 &= -2 \\ -x_2 - x_3 + 2x_4 &= -2 \\ 2x_1 + 3x_2 + 3x_3 + 3x_4 &= -1 \end{aligned}$$

2.

$$\begin{aligned} 2x_1 + 2x_2 - x_3 &= 3 \\ 2x_1 + x_2 - x_4 &= 1 \\ 4x_1 + 2x_2 + x_3 &= 3 \\ 2x_1 + x_2 + x_3 + x_4 &= 2 \end{aligned}$$

3.

$$\begin{aligned} 2x_1 + x_2 - 2x_4 &= 2 \\ 3x_1 + 2x_2 - 2x_3 + x_4 &= 1 \\ -x_1 - x_2 + 2x_3 - 3x_4 &= 1 \\ 3x_3 - x_1 &= 2 \end{aligned}$$

4.

$$\begin{aligned} 2x_1 + 2x_2 + x_3 - x_4 &= 0 \\ 2x_1 + 3x_3 + x_4 &= 0 \\ 3x_1 + 3x_2 + 5x_3 + 2x_4 &= 0 \end{aligned}$$

5.

$$\begin{aligned} x_1 + x_2 - x_3 - x_4 &= 1 \\ 2x_1 - 2x_2 - 2x_3 + 2x_4 &= -2 \\ -3x_1 - 3x_2 + 3x_3 + 3x_4 &= -3 \\ -4x_1 + 4x_2 + 4x_3 - 4x_4 &= 4 \end{aligned}$$

6.

$$\begin{aligned} 2x_1 + 2x_2 + x_3 &= 1 \\ 2x_2 + 2x_3 + x_4 &= -1 \\ x_1 + 2x_3 + 2x_4 &= 1 \\ 2x_1 + x_3 - x_4 &= 0 \end{aligned}$$

7.

$$\begin{aligned} 2x_1 + x_2 - x_4 &= 4, \\ 2x_1 + x_3 - x_4 &= 3, \\ -2x_1 + x_2 + 3x_4 &= -4, \\ x_2 + x_3 + 2x_4 &= -1 \end{aligned}$$

8.

$$\begin{aligned} 2x_1 + 2x_2 + x_3 - 2x_4 &= 2 \\ 2x_1 + x_3 + x_4 &= 2 \\ 3x_4 - 2x_2 &= 0 \end{aligned}$$

9.

$$\begin{aligned} 2x_1 + 2x_2 + x_3 - 2x_4 &= 2 \\ 2x_1 + x_3 + x_4 &= 1 \\ 2x_2 - 3x_4 &= 1 \end{aligned}$$

10.

$$\begin{aligned} 2x_1 + 2x_2 + x_3 &= 1 \\ 2x_2 + 2x_3 + x_4 &= -1 \\ x_1 + 2x_3 + 2x_4 &= 1 \\ 2x_1 - x_3 - x_4 &= 2 \end{aligned}$$

11.

$$\begin{aligned} 2x_1 + x_2 + x_3 &= 3 \\ 2x_2 + 3x_3 + x_4 &= 3 \\ 2x_1 - x_2 - 2x_3 - x_4 &= 0 \\ 2x_2 + x_3 - x_4 &= 9 \end{aligned}$$

12.

$$\begin{aligned} 2x_1 + x_2 - x_4 &= 0 \\ 3x_1 + 2x_2 - 2x_3 + x_4 &= 3 \\ -x_1 - x_2 + 2x_3 - 2x_4 &= -3 \\ 3x_1 + 2x_2 + x_3 - 2x_4 &= 0 \end{aligned}$$

13.

$$\begin{aligned} 2x_1 + x_2 + x_3 &= 1 \\ 2x_2 + 3x_3 + x_4 &= -2 \\ 2x_1 - x_2 - 2x_3 - x_4 &= 3 \\ 2x_1 - x_3 - x_4 &= 2 \end{aligned}$$

14.

$$\begin{aligned} 2x_1 + x_2 + 2x_3 + x_4 &= 2, \\ 3x_1 + x_3 - x_4 &= 4, \\ -2x_1 + x_2 + 3x_4 &= -4, \\ x_1 + x_2 + x_3 + 2x_4 &= 0. \end{aligned}$$

15.

$$\begin{aligned} 2x_1 + x_2 + x_3 &= 1 \\ 2x_2 + 3x_3 + x_4 &= -2 \\ 2x_1 - x_2 - 2x_3 - x_4 &= 3 \\ 2x_2 + x_3 - x_4 &= -2 \end{aligned}$$

16.

$$\begin{aligned} 2x_1 + x_2 + x_3 - x_4 &= 2 \\ 4x_1 + x_2 + x_3 &= 2 \\ 2x_1 + x_4 &= 0 \\ -x_2 - x_3 + 2x_4 &= -2 \end{aligned}$$

17.

$$\begin{aligned} 2x_1 + x_3 - x_4 &= 1 \\ 3x_1 + x_2 + 2x_3 + x_4 &= 1 \\ x_1 + x_2 + x_3 + 2x_4 &= 0 \\ 2x_1 + 2x_2 + x_3 + 5x_4 &= 1 \end{aligned}$$

18.

$$\begin{aligned} 2x_1 + x_2 + 2x_3 + x_4 &= 3, \\ 3x_1 + x_2 - x_3 - x_4 &= 3, \\ -x_1 + 3x_3 + 2x_4 &= 0, \\ 2x_1 + x_2 + x_3 &= 3. \end{aligned}$$

19.

$$\begin{aligned} 2x_1 + x_2 + x_3 + x_4 &= 2, \\ 3x_1 + x_3 - x_4 &= 5, \\ -2x_1 + x_2 + 3x_4 &= -5, \\ x_1 + x_2 + x_3 + 2x_4 &= 0. \end{aligned}$$

20.

$$\begin{aligned} 2x_1 + 2x_2 + x_3 &= 1 \\ 2x_2 + 2x_3 + x_4 &= -1 \\ 3x_1 + x_3 + x_4 &= 3 \\ 2x_1 - x_3 - x_4 &= 2 \end{aligned}$$

21.

$$\begin{aligned} 2x_1 + 2x_2 + x_3 - x_4 &= 2 \\ 2x_1 + 3x_3 + x_4 &= 0 \\ 3x_1 + 3x_2 + 5x_3 + 2x_4 &= 3 \end{aligned}$$

22.

$$\begin{aligned} 2x_1 + x_2 + x_3 + x_4 &= 2, \\ 3x_1 + x_3 - x_4 &= 5, \\ -2x_1 + x_2 + 3x_4 &= -5, \\ 2x_1 + x_2 + x_3 + 2x_4 &= 1. \end{aligned}$$

23.

$$\begin{aligned} 2x_1 + x_2 + 3x_3 - x_4 &= 1 \\ 2x_1 + 3x_2 + 4x_3 + 2x_4 &= 4 \\ 3x_1 + x_2 + x_3 + x_4 &= 4 \end{aligned}$$

24.
$$\begin{aligned} 2x_1 + x_2 + x_3 &= 1 \\ 2x_2 + 3x_3 + x_4 &= -2 \\ 2x_1 - x_2 - 2x_3 - x_4 &= 3 \\ 4x_1 - x_3 - x_4 &= 4 \end{aligned}$$
25.
$$\begin{aligned} 2x_1 + 2x_3 - x_4 &= -1 \\ 2x_1 - x_2 + 3x_3 + x_4 &= 0 \\ 3x_1 + 3x_2 + 2x_4 &= 5 \end{aligned}$$
26.
$$\begin{aligned} 2x_1 + 2x_2 - x_3 &= -1 \\ 2x_1 + x_2 - x_4 &= 0 \\ 4x_1 + 2x_2 + x_3 &= 3 \\ 2x_1 + x_2 + x_3 + x_4 &= 3 \end{aligned}$$
27.
$$\begin{aligned} 2x_1 + x_2 + x_3 + x_4 &= 2 \\ 4x_1 + x_2 + x_3 &= 2 \\ 2x_1 - x_4 &= 0 \\ -x_2 - x_3 - 2x_4 &= -2 \end{aligned}$$
28.
$$\begin{aligned} 2x_1 + x_2 + 3x_3 - x_4 &= 1 \\ 2x_1 + 3x_2 + 2x_3 + 2x_4 &= 4 \\ 2x_2 - x_3 + 3x_4 &= 3 \\ 2x_1 + 2x_2 - x_3 - 3x_4 &= -1 \end{aligned}$$
29.
$$\begin{aligned} 2x_1 + 2x_3 - x_4 &= -1 \\ 2x_1 - x_2 + 3x_3 &= -1 \\ 3x_1 + 3x_2 + 2x_4 &= 5 \end{aligned}$$
30.
$$\begin{aligned} 2x_1 + x_3 - x_4 &= 2 \\ 3x_1 + x_2 + 2x_3 + x_4 &= 1 \\ x_1 + x_2 + x_3 + 2x_4 &= -1 \\ x_1 + 2x_2 + 2x_3 + 5x_4 &= -4 \end{aligned}$$
31.
$$\begin{aligned} 2x_1 + x_2 + 2x_3 - x_4 &= 4, \\ 3x_1 + x_3 - x_4 &= 4, \\ -2x_1 + x_2 + 3x_4 &= -4, \\ x_1 + x_2 + x_3 + 2x_4 &= 0. \end{aligned}$$
32.
$$\begin{aligned} 2x_1 + x_2 + x_3 - x_4 &= 0 \\ 3x_1 + x_2 + 2x_3 &= 2 \\ 2x_1 + x_4 &= 3 \\ -x_2 - x_3 + 2x_4 &= 3 \\ 2x_1 + 3x_2 + 3x_3 + 3x_4 &= 2 \end{aligned}$$
33.
$$\begin{aligned} 2x_1 - 2x_2 + 3x_3 - x_4 &= 2 \\ 4x_1 - 2x_2 + 2x_3 + x_4 &= 3 \\ 2x_1 - x_3 + 2x_4 &= 1 \\ -2x_2 + 4x_3 - 3x_4 &= 1 \end{aligned}$$
34.
$$\begin{aligned} 2x_1 + x_2 + x_3 - x_4 &= 2 \\ 4x_1 + x_2 + x_3 &= 1 \\ 2x_1 + x_4 &= -1 \\ -x_2 - x_3 + 2x_4 &= -3 \\ 2x_1 + 3x_2 + 3x_3 + 3x_4 &= 0 \end{aligned}$$
35.
$$\begin{aligned} x_1 + 2x_2 + 3x_3 + 4x_4 &= 4, \\ 2x_1 + x_2 - x_4 &= 2, \\ 3x_1 + 3x_2 + 3x_3 + 3x_4 &= 6, \\ -x_1 + x_2 + 3x_3 + 5x_4 &= 2. \end{aligned}$$
36.
$$\begin{aligned} 2x_1 + x_2 - x_4 &= 3 \\ 2x_1 - 2x_3 + 2x_4 &= 0 \\ -3x_2 + 3x_3 + 3x_4 &= -3 \\ -4x_1 + 4x_2 + 4x_3 &= -4 \end{aligned}$$
37.
$$\begin{aligned} 2x_1 + x_3 - x_4 &= 1 \\ 3x_1 + x_2 + 2x_3 + x_4 &= 1 \\ 2x_1 - x_2 + 2x_3 + 3x_4 &= 0 \\ 2x_1 + 2x_2 + x_4 &= 2 \end{aligned}$$
38.
$$\begin{aligned} 2x_1 + 2x_2 + x_3 - x_4 &= -1 \\ 2x_1 + 3x_3 + x_4 &= -1 \\ 2x_3 + 2x_4 &= -2 \end{aligned}$$
39.
$$\begin{aligned} 3x_1 + 2x_2 + x_3 &= 4 \\ 3x_2 + 2x_3 + x_4 &= 2 \\ 3x_1 - x_2 - x_3 - x_4 &= 2 \\ x_2 + 2x_3 + 3x_4 &= 2 \end{aligned}$$
40.
$$\begin{aligned} 4x_1 + 2x_2 + x_3 - x_4 &= -1 \\ 3x_1 + 3x_3 + x_4 &= -1 \\ 2x_1 - 2x_2 + 2x_3 + 2x_4 &= 0 \end{aligned}$$
41.
$$\begin{aligned} 2x_1 - 2x_2 + 3x_3 - x_4 &= 0 \\ 4x_1 - 2x_2 + 2x_3 + x_4 &= 1 \\ 2x_1 - x_3 + 2x_4 &= 1 \\ -2x_2 + 4x_3 - 3x_4 &= -1 \end{aligned}$$
42.
$$\begin{aligned} 2x_1 + x_2 + 3x_3 - x_4 &= -2 \\ 2x_1 + 3x_2 + 4x_3 + 2x_4 &= 0 \\ 3x_1 + x_2 + x_3 + x_4 &= 3 \end{aligned}$$
43.
$$\begin{aligned} 2x_1 + x_2 + x_3 + x_4 &= 2 \\ 4x_1 + x_3 + x_4 &= 1 \\ 2x_1 - x_2 &= -1 \\ -2x_2 - x_3 - x_4 &= -3 \end{aligned}$$
44.
$$\begin{aligned} 3x_1 + 2x_2 - x_3 + 2x_4 &= 2 \\ 3x_2 + 2x_3 + 3x_4 &= 2 \\ 3x_1 - x_2 - 3x_3 - x_4 &= 0 \end{aligned}$$
45.
$$\begin{aligned} 2x_1 - 2x_2 + x_3 - x_4 &= -1 \\ 4x_1 - 2x_2 + x_3 + x_4 &= -1 \\ 2x_1 + 2x_4 &= 0 \\ -2x_2 + x_3 - 3x_4 &= -1 \end{aligned}$$
46.
$$\begin{aligned} 2x_1 + x_3 - x_4 &= 1 \\ 3x_1 + x_2 + 2x_3 + x_4 &= 1 \\ x_1 + x_2 + x_3 + 2x_4 &= 0 \\ x_1 + 2x_2 + x_3 + 5x_4 &= 0 \end{aligned}$$
47.
$$\begin{aligned} 2x_1 + 2x_3 - x_4 &= -1 \\ 2x_1 - x_2 + 3x_3 &= -1 \\ 3x_1 + 3x_2 + x_4 &= 4 \end{aligned}$$
48.
$$\begin{aligned} 2x_1 + x_2 - x_3 &= 1 \\ 3x_1 + 2x_2 - 2x_3 + x_4 &= 3 \\ -x_1 + 2x_2 + 2x_3 - 3x_4 &= -1 \\ 2x_1 + 4x_2 - 2x_4 &= 2 \end{aligned}$$
49.
$$\begin{aligned} 2x_1 + x_2 + x_3 - x_4 &= 2 \\ 4x_1 + x_2 + x_3 &= 1 \\ 2x_1 + x_4 &= -1 \\ -x_2 - x_3 + 2x_4 &= -3 \end{aligned}$$
50.
$$\begin{aligned} 3x_1 + 2x_2 - x_3 + 2x_4 &= 2 \\ 3x_2 + 2x_3 + 3x_4 &= 2 \\ 3x_1 - x_2 - 3x_3 - x_4 &= 0 \\ 3x_1 - x_3 &= 2 \end{aligned}$$

Vyřešte soustavu rovnic

1.

$$x_1 = 1, x_2 = 1, x_3 = -1, x_4 = -1, s, t \in \mathbb{R}.$$

2.

$$x_1 = -1+2t, x_2 = 3-3t, x_3 = 1-2t, x_4 = t, t \in \mathbb{R}.$$

3.

$$x_1 = 1+3t, x_2 = -4t, x_3 = 1+t, x_4 = t, t \in \mathbb{R}.$$

4.

$$x_1 = t, x_2 = 0, x_3 = -t, x_4 = t, t \in \mathbb{R}.$$

5.

$$x_1 = 0+t, x_2 = 1+s, x_3 = t, x_4 = s, s, t \in \mathbb{R}.$$

6.

$$x_1 = 1, x_2 = 0, x_3 = -1, x_4 = 1.$$

7.

$$x_1 = 2+t, x_2 = -t, x_3 = -1-t, x_4 = t, t \in \mathbb{R}.$$

8.

$$x_1 = 1-s-t, x_2 = 3s+2t, x_3 = 2t, x_4 = 2s, s, t \in \mathbb{R}.$$

9.

$$x_1 = \frac{1}{2}-s-t, x_2 = \frac{1}{2}+3s, x_3 = 2t, x_4 = 2s, s, t \in \mathbb{R}.$$

10.

$$x_1 = 1, x_2 = -\frac{1}{2}+t, x_3 = -2t, x_4 = 2t, t \in \mathbb{R}.$$

11.

$$x_1 = 0, x_2 = 6+t, x_3 = -3-t, x_4 = t, t \in \mathbb{R}.$$

12.

$$x_1 = -1+t, x_2 = 2-t, x_3 = -1+t, x_4 = t, t \in \mathbb{R}.$$

13.

$$x_1 = 1, x_2 = -1+t, x_3 = -t, x_4 = t, t \in \mathbb{R}.$$

14.

$$x_1 = 1, x_2 = -2-3t, x_3 = 1+t, x_4 = t, t \in \mathbb{R}.$$

15.

$$x_1 = 1, x_2 = -1+t, x_3 = -t, x_4 = t, t \in \mathbb{R}.$$

16.

$$x_1 = s, x_2 = 2-4s-t, x_3 = t, x_4 = 2s, s, t \in \mathbb{R}.$$

17.

$$x_1 = 1, x_2 = -3t, x_3 = -1+t, x_4 = t, t \in \mathbb{R}.$$

18.

$$x_1 = -t, x_2 = 3+3t, x_3 = -t, x_4 = t, s, t \in \mathbb{R}.$$

19.

$$x_1 = 2+t, x_2 = -1-t, x_3 = -1-2t, x_4 = t, t \in \mathbb{R}.$$

20.

$$x_1 = 1, x_2 = \frac{1}{2}+t, x_3 = -2t, x_4 = 2t, t \in \mathbb{R}.$$

21.

$$x_1 = t, x_2 = 1, x_3 = -t, x_4 = t, t \in \mathbb{R}.$$

22.

$$x_1 = 1, x_2 = 0, x_3 = 1, x_4 = -1.$$

23.

$$x_1 = 1, x_2 = 2-2t, x_3 = -1+t, x_4 = t, t \in \mathbb{R}.$$

24.

$$x_1 = 1+t+s, x_2 = -1-2t-6t, x_3 = 4s, x_4 = 4t, s, t \in \mathbb{R}.$$

25.

$$x_1 = -t, x_2 = 1+t, x_3 = t, x_4 = 1, t \in \mathbb{R}.$$

26.

$$x_1 = -1+2t, x_2 = 2-3t, x_3 = 3-2t, x_4 = t, t \in \mathbb{R}.$$

27.

$$x_1 = s, x_2 = 2-4s-t, x_3 = t, x_4 = 2s, s, t \in \mathbb{R}.$$

28.

$$x_1 = -2+t, x_2 = 2-2t, x_3 = 1-t, x_4 = t, t \in \mathbb{R}.$$

29.

$$x_1 = -t, x_2 = 1+t, x_3 = t, x_4 = 1, t \in \mathbb{R}.$$

30.

$$x_1 = 2+t, x_2 = -1-2t, x_3 = -2-t, x_4 = t, t \in \mathbb{R}.$$

31.

$$x_1 = 1-t, x_2 = 1-5t, x_3 = 4t, x_4 = t, t \in \mathbb{R}.$$

32.

$$x_1 = 1, x_2 = -1, x_3 = 0, x_4 = 1, s, t \in \mathbb{R}.$$

42.

$$x_1 = 1, x_2 = 2 - 2t, x_3 = -2 + t, x_4 = t, s, t \in \mathbb{R}.$$

33.

$$x_1 = \frac{1}{2} - 2s + t, x_2 = \frac{1}{2} - 3s + 4t, x_3 = 2t, x_4 = 2s, s, t \in \mathbb{R}$$

43.

$$x_1 = \frac{1}{4} - s - t, x_2 = \frac{3}{2} - 2s - 2t, x_3 = 4t, x_4 = 4s, s, t \in \mathbb{R}.$$

34.

$$x_1 = 0, x_2 = 1 - t, x_3 = t, x_4 = -1, t \in \mathbb{R}.$$

44.

$$x_1 = \frac{2}{9} + 7t, x_2 = \frac{2}{3} - s - 6t, x_3 = 9t, x_4 = s, s, t \in \mathbb{R}.$$

35.

$$x_1 = 2s + t, x_2 = 2 - 3s - 2t, x_3 = t, x_4 = s, s, t \in \mathbb{R}.$$

45.

$$x_1 = -2s, x_2 = \frac{1}{2} - 3s + t, x_3 = 2t, x_4 = 2s, s, t \in \mathbb{R}.$$

36.

$$x_1 = 1, x_2 = 0, x_3 = 0, x_4 = -1.$$

46.

$$x_1 = 1, x_2 = -3t, x_3 = -1 + t, x_4 = t, t \in \mathbb{R}.$$

37.

$$x_1 = 1, x_2 = 0, x_3 = -1, x_4 = 0.$$

47.

$$x_1 = -t, x_2 = 1 + t, x_3 = t, x_4 = 1, t \in \mathbb{R}.$$

38.

$$x_1 = 1 + t, x_2 = -1, x_3 = -1 - t, x_4 = t, t \in \mathbb{R}.$$

48.

$$x_1 = -1 + t, x_2 = 1, x_3 = -2 + 2t, x_4 = t, t \in \mathbb{R}.$$

39.

$$x_1 = 1, x_2 = t, x_3 = 1 - 2t, x_4 = t, t \in \mathbb{R}.$$

49.

$$x_1 = 0, x_2 = -1 + 2t, x_3 = -t, x_4 = -1 + 3t, t \in \mathbb{R}. \quad x_1 = -\frac{1}{2} + s, x_2 = 3 - 4s - t, x_3 = t, x_4 = 2s, s, t \in \mathbb{R}.$$

41.

$$x_1 = \frac{1}{2} - 2s + t, x_2 = \frac{1}{2} - 3s + 4t, x_3 = 2t, x_4 = 2t, s, t \in \mathbb{R}. \quad x_1 = 1, x_2 = -t, x_3 = 1, x_4 = t, t \in \mathbb{R}.$$

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