

**Vyřešte soustavu rovnic**

1. 
$$\begin{aligned} 2x_1 + 2x_2 - x_3 + x_4 &= 0 \\ 3x_1 - x_2 + x_4 &= 0 \\ 3x_1 - 2x_2 - 2x_3 + 2x_4 &= 0 \\ -3x_1 + 10x_2 - x_3 - x_4 &= 0 \end{aligned}$$
2. 
$$\begin{aligned} -3x_1 - x_2 + x_3 + 3x_4 &= 0 \\ 2x_1 + 2x_2 - 2x_3 - 2x_4 &= 0 \\ -x_1 - 3x_2 + 3x_3 + x_4 &= 0 \\ 3x_2 + 2x_3 + 5x_4 &= 0 \end{aligned}$$
3. 
$$\begin{aligned} x_1 - x_3 + x_4 &= 0 \\ 2x_1 + 3x_2 + x_4 &= 0 \\ 3x_1 + 3x_2 - x_3 + 2x_4 &= 0 \\ 2x_1 + 3x_2 + 2x_4 &= 0 \end{aligned}$$
4. 
$$\begin{aligned} 2x_2 - x_3 + 2x_4 &= 0 \\ 3x_1 - x_2 + 2x_3 + x_4 &= 0 \\ 3x_1 + x_2 + x_3 + 3x_4 &= 0 \\ 3x_1 + 3x_2 + 5x_4 &= 0 \end{aligned}$$
5. 
$$\begin{aligned} -x_1 - x_3 + x_4 &= 0 \\ 2x_1 + 2x_2 - x_3 + 2x_4 &= 0 \\ 2x_2 - 3x_3 + 4x_4 &= 0 \\ -9x_1 - 6x_2 + x_3 &= 0 \\ -x_1 - 2x_2 + 3x_3 &= 0 \end{aligned}$$
6. 
$$\begin{aligned} 2x_2 + x_3 + 2x_4 &= 0 \\ 3x_1 + x_2 + 2x_3 + x_4 &= 0 \\ x_1 + x_2 + x_3 + x_4 &= 0 \\ x_1 + 3x_2 + 2x_3 + 3x_4 &= 0 \end{aligned}$$
7. 
$$\begin{aligned} 2x_1 + 2x_2 - x_3 + 2x_4 &= 0 \\ x_1 - x_2 + x_4 &= 0 \\ 3x_1 + x_2 - x_3 + 3x_4 &= 0 \end{aligned}$$
8. 
$$\begin{aligned} 2x_1 + x_2 - x_3 + x_4 &= 0 \\ 3x_1 - 2x_2 + x_4 &= 0 \\ 3x_1 - 4x_2 - 2x_3 + 2x_4 &= 0 \\ -3x_1 + 11x_2 - x_3 - x_4 &= 0 \\ -x_1 + 5x_2 + x_3 - x_4 &= 0 \end{aligned}$$
9. 
$$\begin{aligned} x_1 + 2x_2 - x_3 + x_4 &= 0 \\ 2x_1 + 3x_2 + x_3 + 3x_4 &= 0 \\ 3x_1 - x_2 - 3x_3 - x_4 &= 0 \\ 2x_1 + 2x_2 + x_4 &= 0 \end{aligned}$$
10. 
$$\begin{aligned} x_1 + 2x_2 + 3x_3 + 4x_4 &= 0 \\ 4x_1 + 3x_2 + 2x_3 + x_4 &= 0 \\ 2x_1 + x_2 + 4x_3 + 3x_4 &= 0 \\ 3x_1 + 4x_2 + x_3 + 2x_4 &= 0 \end{aligned}$$
11. 
$$\begin{aligned} 2x_1 + 2x_2 - x_3 &= 0 \\ x_1 - x_2 + x_3 &= 0 \\ 3x_1 + x_2 &= 0 \\ 2x_1 + 3x_2 - x_3 &= 0 \end{aligned}$$
12. 
$$\begin{aligned} 3x_1 + 2x_2 - x_3 + x_4 &= 0 \\ 3x_2 + 2x_3 + 3x_4 &= 0 \\ 3x_1 - x_2 - 3x_3 - x_4 &= 0 \end{aligned}$$
13. 
$$\begin{aligned} 2x_2 - x_3 + 2x_4 &= 0 \\ 3x_1 - x_2 + 2x_3 + x_4 &= 0 \\ 3x_1 + x_2 + x_3 + 3x_4 &= 0 \\ x_1 + 2x_3 + 3x_4 &= 0 \end{aligned}$$
14. 
$$\begin{aligned} x_1 + 2x_2 - x_3 + x_4 &= 0 \\ 2x_1 + 3x_2 + 2x_3 + 3x_4 &= 0 \\ 3x_1 - x_2 - 3x_3 - x_4 &= 0 \end{aligned}$$
15. 
$$\begin{aligned} 2x_1 - x_3 + 3x_4 &= 0 \\ 4x_1 - x_2 + x_3 + 4x_4 &= 0 \\ 10x_1 - 2x_2 + x_3 + 11x_4 &= 0 \\ -2x_1 + 3x_2 - 8x_3 + 3x_4 &= 0 \\ x_2 - 3x_3 + 2x_4 &= 0 \end{aligned}$$
16. 
$$\begin{aligned} 3x_1 + 2x_2 - x_3 + 2x_4 &= 0 \\ 3x_1 + 3x_2 - x_3 + 2x_4 &= 0 \\ x_2 + x_4 &= 0 \end{aligned}$$
17. 
$$\begin{aligned} 2x_2 - x_3 + 2x_4 &= 0 \\ 3x_1 - x_2 + 2x_3 + x_4 &= 0 \\ 3x_1 + x_2 + x_3 + 3x_4 &= 0 \\ 2x_1 + 2x_2 + 2x_4 &= 0 \end{aligned}$$
18. 
$$\begin{aligned} 2x_1 + 2x_2 - x_3 &= 0 \\ x_1 - x_2 + x_3 &= 0 \\ 3x_1 + x_2 &= 0 \\ 2x_1 + 2x_2 - x_3 &= 0 \end{aligned}$$
19. 
$$\begin{aligned} x_1 + 2x_2 - x_3 + 2x_4 &= 0 \\ 3x_1 + 3x_2 - x_3 + 2x_4 &= 0 \\ 2x_1 + 2x_2 + x_3 + x_4 &= 0 \end{aligned}$$
20. 
$$\begin{aligned} 2x_2 - x_3 + 2x_4 &= 0 \\ 3x_1 - x_2 + x_4 &= 0 \\ 3x_1 + x_2 - x_3 + 3x_4 &= 0 \\ 3x_1 + 3x_2 - 2x_3 + 5x_4 &= 0 \end{aligned}$$
21. 
$$\begin{aligned} 3x_1 + 2x_2 - x_3 + 2x_4 &= 0 \\ 3x_1 + 3x_2 + x_3 + x_4 &= 0 \\ x_2 + 2x_3 - x_4 &= 0 \end{aligned}$$
22. 
$$\begin{aligned} 3x_1 + 2x_2 - x_3 + 2x_4 &= 0 \\ 3x_1 + 2x_3 + x_4 &= 0 \\ 2x_1 + x_2 + 2x_3 - x_4 &= 0 \\ 2x_1 - 2x_2 + 4x_4 &= 0 \end{aligned}$$
23. 
$$\begin{aligned} 2x_1 + 2x_2 - x_3 &= 0 \\ x_1 - x_2 + x_3 &= 0 \\ x_1 - x_2 + 3x_3 &= 0 \\ 2x_1 + 3x_2 + x_3 &= 0 \end{aligned}$$
24. 
$$\begin{aligned} x_1 - x_3 + x_4 &= 0 \\ 3x_1 + 3x_2 - x_3 + 2x_4 &= 0 \\ 2x_1 + 2x_2 + x_4 &= 0 \\ -2x_1 - 6x_2 - 2x_3 &= 0 \end{aligned}$$
25. 
$$\begin{aligned} -x_1 - x_3 + x_4 &= 0 \\ 2x_1 + 2x_2 - x_3 + 2x_4 &= 0 \\ 3x_1 + 4x_2 - 3x_3 + 5x_4 &= 0 \\ -11x_1 - 6x_2 - 2x_3 - x_4 &= 0 \\ -4x_1 - 2x_2 - x_3 &= 0 \end{aligned}$$

**Vyřešte soustavu rovnic**

1.

$$x_1 = -6r, x_2 = r, x_3 = 9r, x_4 = 19r, \quad r \in \mathbb{R}.$$

14.

$$x_1 = -7r, x_2 = -16r, x_3 = -11r, x_4 = 28r, \quad r \in \mathbb{R},$$

2.

$$x_1 = r, x_2 = -r, x_3 = -r, x_4 = r, \quad r \in \mathbb{R}.$$

15.

$$x_1 = s - 3r, x_2 = 6s - 4r, x_3 = 2s, x_4 = 2r, \quad r, s \in \mathbb{R}.$$

3.

$$x_1 = 3r, x_2 = -2r, x_3 = 3r, x_4 = 0, \quad r, s, t \in \mathbb{R},$$

16.

$$x_1 = r, x_2 = 0, x_3 = 3r, x_4 = 0, \quad r \in \mathbb{R}.$$

4.

$$x_1 = -2r - s, x_2 = s - 3r, x_3 = 2s, x_4 = 3r, \quad r, s \in \mathbb{R}$$

$$x_1 = -r, x_2 = r, x_3 = 2r, x_4 = 0, \quad r \in \mathbb{R}.$$

5.

$$x_1 = 8r, x_2 = -13r, x_3 = -6r, \quad , s, t \in \mathbb{R}.$$

18.

$$x_1 = -r, x_2 = 3r, x_3 = 4r, \quad r \in \mathbb{R}.$$

6.

$$x_1 = -s, x_2 = -r - s, x_3 = 2s, x_4 = r, \quad r, s \in \mathbb{R}.$$

19.

$$x_1 = 3r, x_2 = -6r, x_3 = r, x_4 = 5r, \quad r \in \mathbb{R}.$$

7.

$$x_1 = s - r, x_2 = s, x_3 = 4s, x_4 = r, \quad r, s \in \mathbb{R}.$$

20.

$$x_1 = s - 2r, x_2 = 3s - 3r, x_3 = 6s, x_4 = 3r, \quad r, s \in \mathbb{R}.$$

8.

$$x_1 = -6r, x_2 = r, x_3 = 9r, x_4 = 20r, \quad r \in \mathbb{R}.$$

21.

$$x_1 = 5s - 4r, x_2 = 3r - 6s, x_3 = 3s, x_4 = 3r, \quad r, s \in \mathbb{R}.$$

9.

$$x_1 = 0, x_2 = 0, x_3 = 0, x_4 = 0.$$

22.

$$x_1 = -r, x_2 = r, x_3 = r, x_4 = r, \quad r \in \mathbb{R}.$$

10.

$$x_1 = r, x_2 = -r, x_3 = -r, x_4 = r, \quad r \in \mathbb{R}.$$

23.

$$x_1 = 0, x_2 = 0, x_3 = 0, x_4 = 0.$$

11.

$$x_1 = 0, x_2 = 0, x_3 = 0, x_4 = 0.$$

24.

$$x_1 = -r, x_2 = 0, x_3 = r, x_4 = 2r, \quad r \in \mathbb{R}.$$

12.

$$x_1 = 7r, x_2 = -6r, x_3 = 9r, x_4 = 0, \quad r \in \mathbb{R},$$

25.

$$x_1 = r - 2s, x_2 = 3s - 2r, x_3 = 2s, x_4 = r, \quad r, s \in \mathbb{R}.$$

13.

$$x_1 = r, x_2 = -16r, x_3 = -14r, x_4 = 9r, \quad r \in \mathbb{R}.$$